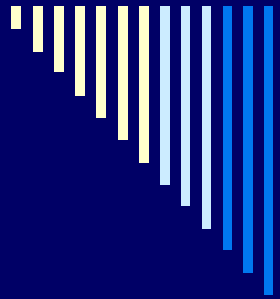


Experimental strategies: An Introduction

From a descriptive view up to study questions

Based on *D. C. Montgomery, Design and Analysis of Experiments*, McGraw-Hill.



What an experiment can prove

No amount of experimentation can ever prove me right; a single experiment can prove me wrong.

Albert Einstein

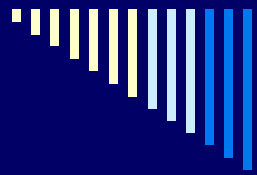
Letter to Max Born, December 4, 1926

Cases without human subjects

We want to show some cases where Exp. Eng. Techniques are applied [quite] without human **subjects** (only MD experiments should have human **objects**).

Valutare, al fine di ottenere, a parità di tutto il resto:

- +10% della durezza da tempera di alluminio in bagni {B1, B2, B3} e con temperature {T1, T2}
- - 3% scarti da saldatura componenti elettronici su circuito stampato con tecniche {S1, S2}



A case with human subjects

We want to show a case where Exp. Sw. Eng. Techniques are applied with human **subjects** (but, of course, without human **objects**).

Valutare, al fine di ridurre del 10% i difetti al rilascio:

- Tecnica I1 e tecnica I2 di ispezione di requisiti software (o codice, etc.)



A case of MD experiment with human objects (and subjects)

We as want to show a case where MD subjects apply Exp. Med. **Treatments** (or **Levels**) of a given Exp. **Factor** to human (as exp. objects).

Valutare impatto su ore/giorno di mal di testa in persone predisposte:

- Somministrazione del principio attivo Xxx in dose di 10 mg, 5 mg 1 o, rispettivamente, 0 mg una volta al giorno.

An ESE example

We would want to understand if it improves in the average the extensive maintenance time of software applications in a given domain using a structured approach to software design.

Input Variables

- Sw. Design (MVC, Ad hoc)
- Others: as usual

– Levels: 1 factor, 2 treatments.



One more ESE example

We would want to understand if it improves in the average the extensive maintenance time of software applications in a given domain using a structured approach to software design, and J2EE, Java, RSA and people with different levels of experience and expertise.

Input Variables

- Sw. Design (MVC, Ad hoc)
- Development technology (J2EE, .NET)
- Programming Languages (Java 2.6, C# 1.5)
- Documentation tools (*UML, RSA)
- Experience of subjects (Junior, Average, Senior)
- Expertise of subjects (Low, Medium, High)
- ...

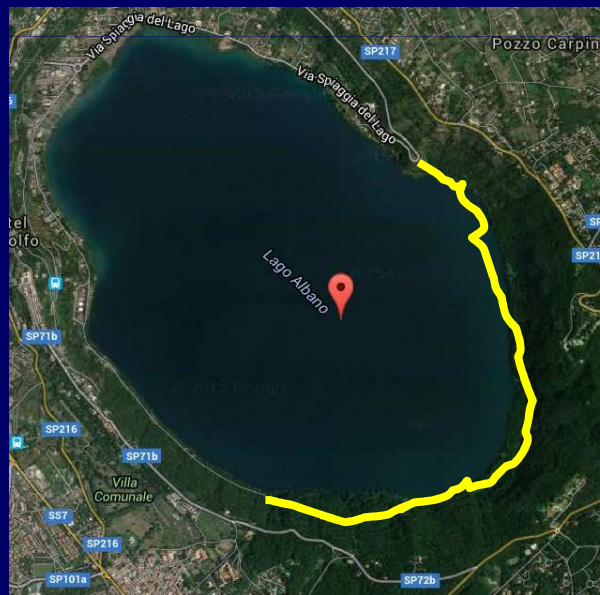
– Levels: 1 out of 2 or 3 for each input variable.

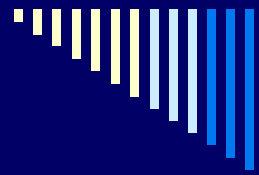


A simple hybrid example

We want to improve the **time** that a team (person) would need in the average to bike two ways the Albano lake's wood path.

Input Variables ?





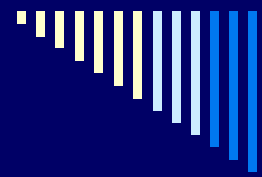
A simple hybrid example

We want to improve the time that a team (person) would need in the average to bike two ways the Albano lake's wood path.

Input Variables

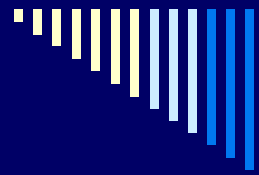
- Bike type (C, MB)
- Rocket rate (S, L)
- Wheel diameter (24, 26)
- Wheel type (L, C)
- Weather (D, W)
- Expertise of subjects (Medium, High)
- ...

Levels: 1 out of 2 for each input variable.

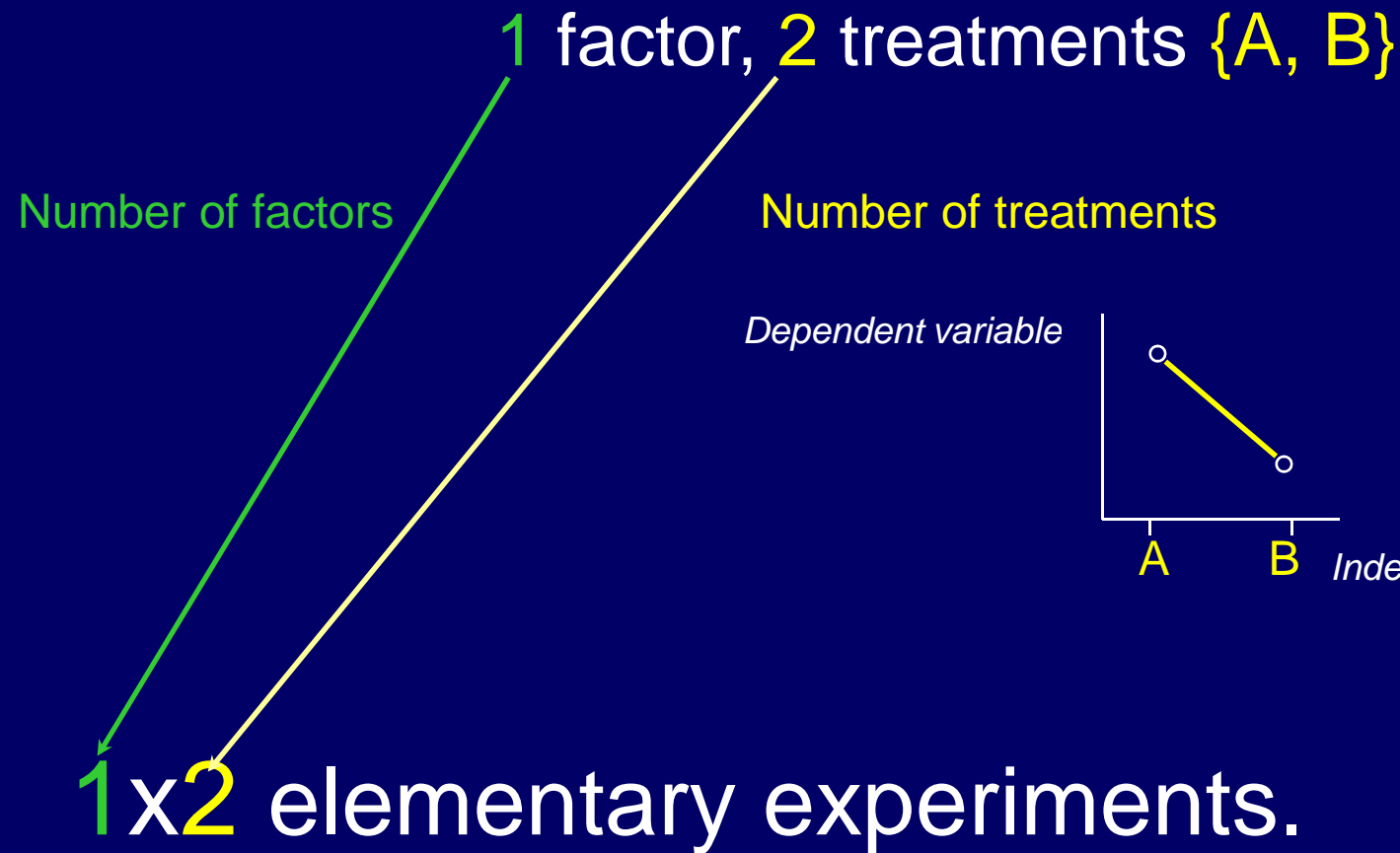


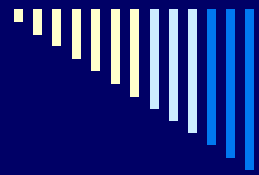
Experimental strategy

- None
- Attempt
- One variable does change
- Factorial (complete, incomplete)
-



Experimental strategy





Experimental strategy

1 factor, 2 treatments {A, B}

Wheel Φ : $\{\Phi 24, \Phi 28\}$

Parameters

INPUT VARIABLES
CONTROLLED AT
CONSTANT LEVELS:

Bike type = MB

Rocket= S

Wheel type= L

Weather= Dry

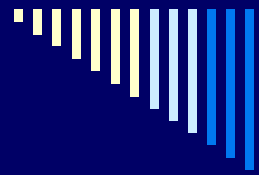
Path experience= H

Time (min)



Wheel Φ

Q: What other about people involved as experimental subjects?



Experimental strategy

1 factor, 2 treatments {A, B}

Style Σ : { Σ MVC, Σ AdHoc}

Parameters

INPUT VARIABLES
CONTROLLED AT
CONSTANT LEVELS:

Dev. Tech. = J2EE

Prg. Lang. = Java

Doc. Tools = {starUML, ...}

Env. = {SQL, Apache, ..}

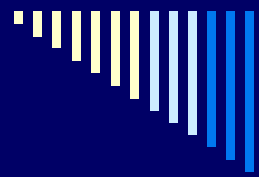
Experience = J

Expertise = M

Time (min)



Q: What other about people involved as experimental subjects?



Experimental strategy

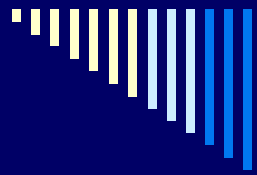
More than one factors ($F_1, F_2, \dots F_n$).
1 factor does change per time



*Four factors ($F_1..F_4$), each with **two treatments***

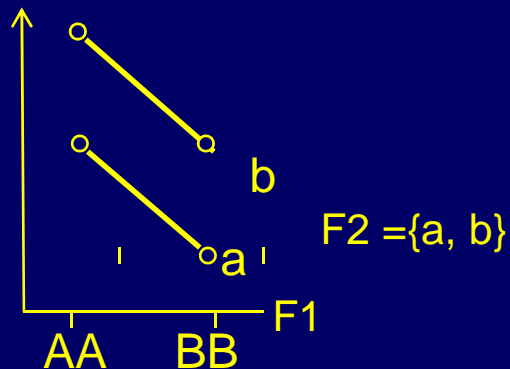
Descriptive result

- If the scale of ordinate is ascending (resp. descending) then the best choice for (F_1, F_3, F_4) is (A, bb, AA) (resp. (B, aa, BB)).*
- F_2 does not affect outcomes for the given constant levels.*



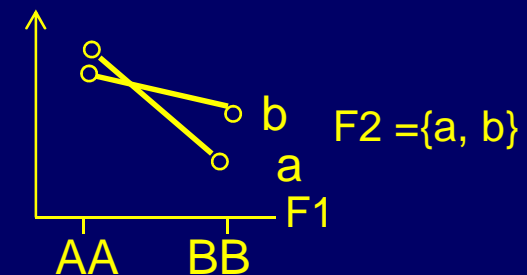
Experimental strategy

Interaction between two factors



Not interacting factors

Best result: (AA, b), ascending Y scale



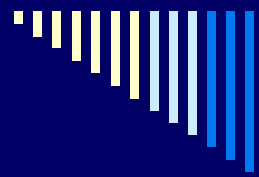
Interacting factors

Best result: (AA, a), ascending Y scale

Two factors, each with **two treatments**

Factors interact when variation in the combinations of treatments do affect outcome variations (Δ)

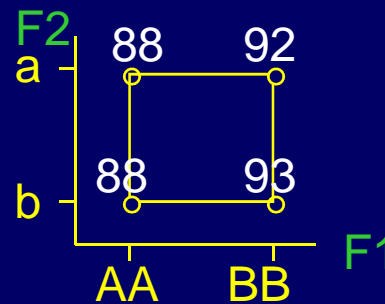
Q: What tools to use to understand whether there is interaction between input variables?



Experimental strategy

Factorial

Number of factors



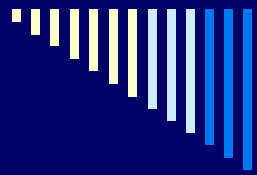
Number of treatments
(or levels)

2 factors, each with 2 treatments (2x2)

$$\text{Effect of } F1 = (92+93)/2 - (88+88)/2 = 4.5$$

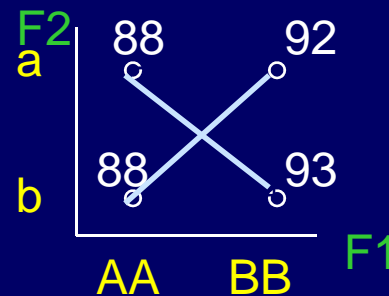
$$\text{Effect of } F2 = (88+93)/2 - (88+92)/2 = 0.5$$

2x2 elementary experiments.



Experimental strategy

Factorial 2x2 Interactions

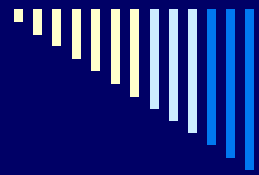


Effect of interaction btw. F1 and F2

$$= (93+88)/2 - (88+92)/2 = 0,5$$

Q: Concerning outcomes, in what % do they depend on F1, F2, F1 and F2 interaction, respectively?

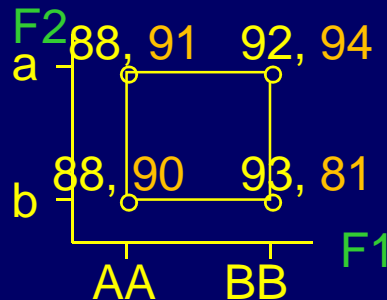
Q: What tools to evaluate the effect of interaction between input variables?



Experimental strategy

Factorial 2x2 + 1 replication

Replications

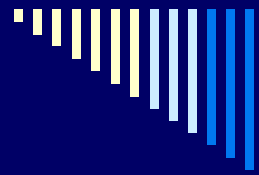


Effect of $F1 = 3,25$ ()*

Effect of $F2 = 0.75$

() = $(92+94+93+81)/4 - (88+91+88+90)/4$*

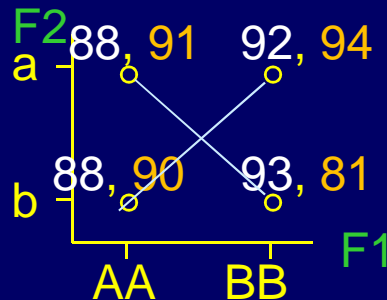
Q: Does replication impact on variance?



Experimental strategy

Factorial 2x2 + 1 replication

Interaction & Replications



Effect of interaction btw. F1 and F2

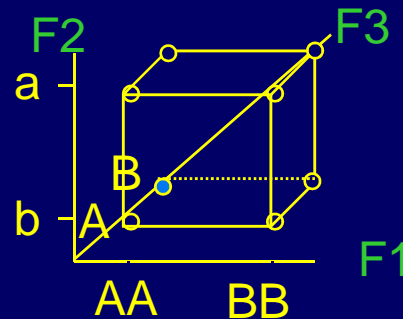
$$= (92 + 94 + 88 + 90) / 4 - (88 + 91 + 93 + 81) / 4 = 0,25$$

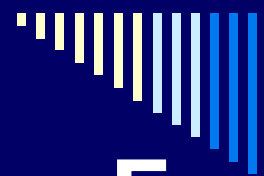
Q: concerning outcomes, in what % do they depend on F1, F2, F1 and F2 interaction, respectively?
Is there an impact on mean and variance?



Experimental strategy

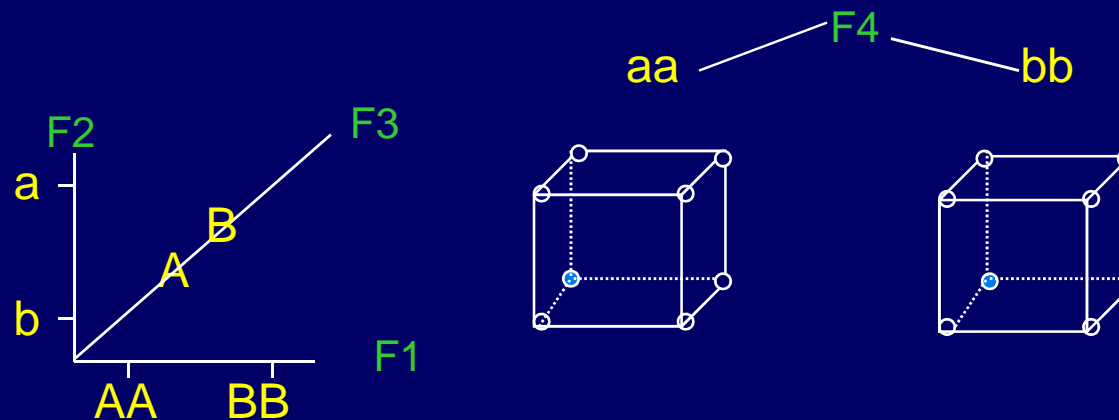
Factorial design with **3 factors**, each with **2 treatments**.

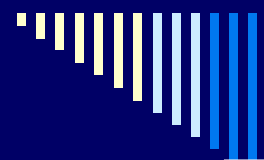




Experimental strategy

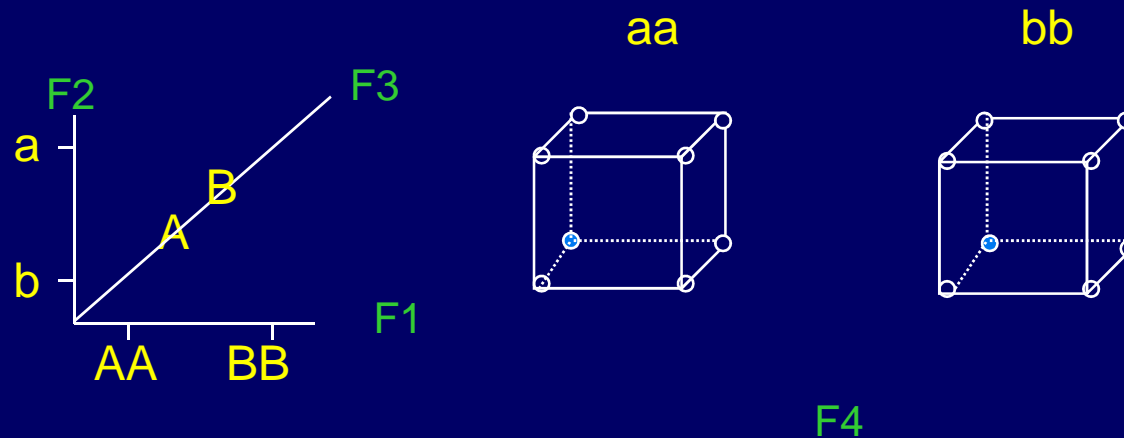
Factorial design with **4 factors**, each with **2 treatments**.





Experimental strategy

Fractional Factorial design with 4 factors, each with 2 treatments.



$\frac{1}{2}$ Fraction